# Structure of Lead Bis(dihydrogenphosphate) 

By P. Vasić<br>Faculty of Priština, University of Priština, 38000 Priština, Yugloslavia<br>and b. Prelesnik, R. Herak and M. Čurić<br>Laboratory of Solid-State Physics and Radiation Chemistry, 'Boris Kidrič' Institute, 11001 Belgrade, PO Box 522, Yugoslavia

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Abstract. $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$, triclinic, $P \overline{1}, a=9.029$ (3), $b=$ $5.863(1), c=7.815(3) \AA, \alpha=96.92(2), \beta=$ 119.56 (3),$\gamma=104.92$ (2) ${ }^{\circ}, V=332.3$ (2) $\AA^{3}, Z=2$, $D_{x}=4.03 \mathrm{Mg} \mathrm{m}^{-3}, \mu(\mathrm{Mo} K a)=25.6 \mathrm{~mm}^{-1}$, final $R=$ 0.099 . The seven shortest $\mathrm{Pb}-\mathrm{O}$ distances are in the range $2.44-2.88 \AA$. Hydrogen-bonded dimers form a three-dimensional network.

Introduction. The investigation of the crystal structure of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ was performed as part of a study of acidic phosphates. To obtain crystals of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$, first $\mathrm{Pb}\left(\mathrm{HPO}_{4}\right)$ was prepared. $\mathrm{PbCO}_{3}$ was added to $50 \% \mathrm{H}_{3} \mathrm{PO}_{4}$ and heated at 353 K until a precipitate began to appear. The solution was then heated at 373 K to dissolve all $\mathrm{PbCO}_{3}$. On cooling, tiny plates of $\mathrm{Pb}\left(\mathrm{HPO}_{4}\right)$ crystallized. The precipitate was washed with water, dried and dissolved in $96 \% \mathrm{H}_{3} \mathrm{PO}_{4}$ at 453 K . By cooling slowly, prismatic needles of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ were obtained. The crystals are sensitive to moisture. The excess of $\mathrm{H}_{3} \mathrm{PO}_{4}$ is difficult to wash out. Treatment with ether, as recommended by Mellor (1947), has no appreciable effect on the stability of the crystals.

For all crystallographic measurements, crystals sealed in Lindemann-glass capillaries were used. Preliminary Weissenberg photographs indicated triclinic symmetry. A crystal of dimensions $0.09 \times 0.14$ $\times 0.28 \mathrm{~mm}$ was mounted on a Syntex $P \overline{1}$ diffractometer. Cell parameters were determined by least squares from $2 \theta$ values for 14 strong general reflexions. The intensity measurements were made by the $\omega$-scan technique, using graphite-monochromated Mo $K \alpha$ radiation. Intensities of 1730 reflexions in the sphere $\theta$ $\leq 30^{\circ}$ which satisfied the criterion $I \geq 3 \sigma(I)$ were used in the subsequent analyses. In the absence of a suitable program no absorption correction was applied.

The structure was solved by the heavy-atom method. Isotropic refinement of the nonhydrogen atoms terminated at $R=0 \cdot 136$. Refinement with anisotropic thermal parameters for Pb led to a non-definite value for the vibrational tensor. The least-squares refinement in space group $P 1$ was unsuccessful. At that stage of

Table 1. Fractional coordinates $\left(\times 10^{5}\right.$ for $\mathrm{Pb}, \times 10^{4}$ for $\mathrm{P}, \mathrm{O}$ ) and thermal parameters

|  | $x$ | $y$ | $z$ | $B_{\text {iso }}\left(\AA^{2}\right)$ |
| :--- | :---: | :---: | :--- | :---: |
|  | $x$ | $y$ |  |  |
| Pb | $7666(9)$ | $24556(12)$ | $11132(10)$ | $*$ |
| $\mathrm{P}(1)$ | $3493(6)$ | $3590(8)$ | $1012(7)$ | $0.64(6)$ |
| $\mathrm{P}(2)$ | $1934(6)$ | $-1368(8)$ | $4176(7)$ | $0.65(6)$ |
| $\mathrm{O}(1)$ | $3904(20)$ | $1672(26)$ | $-94(22)$ | $1.21(21)$ |
| $\mathrm{O}(2)$ | $5334(21)$ | $4724(29)$ | $3253(23)$ | $1.53(23)$ |
| $\mathrm{O}(3)$ | $1899(20)$ | $2008(27)$ | $1094(22)$ | $1.32(21)$ |
| $\mathrm{O}(4)$ | $3221(18)$ | $5605(25)$ | $22(20)$ | $0.97(19)$ |
| $\mathrm{O}(5)$ | $659(20)$ | $-10(27)$ | $3960(22)$ | $1.21(21)$ |
| $\mathrm{O}(6)$ | $1855(20)$ | $-3024(27)$ | $5613(22)$ | $1.25(21)$ |
| $\mathrm{O}(7)$ | $3873(21)$ | $545(28)$ | $5239(23)$ | $1.45(22)$ |
| $\mathrm{O}(8)$ | $1376(19)$ | $-3064(25)$ | $2178(20)$ | $1.01(19)$ |

* Anisotropic thermal parameters $\left(\times 10^{4}\right)$ for the Pb atom, with their e.s.d.'s in parentheses, are: $\beta_{11}=42(1), \beta_{22}=73(2)$, $\beta_{33}=70(2), \beta_{12}=18(1), \beta_{13}=52(1), \beta_{23}=36(1)$.
refinement, $\sigma(I)=99.0$ was ascribed to 76 reflexions. These reflexions, with low $h k l$ indices, exhibited large differences between $F_{o}$ and $F_{c}$ and were considered to be the most affected by absorption. Refinement of the positional and thermal parameters (anisotropic for Pb and isotropic for P and O ) by full-matrix least squares was normal and converged at $R=0.099, R_{w}=0.100$. Scattering factors and anomalous-dispersion corrections for neutral atoms were taken from International Tables for X-ray Crystallography (1974). The main programs used on the CDC-36000 computer were FORDAP, Zalkin's (1965) Fourier program, $N U C L S$, a modification by J. A. Ibers and R. J. Doedens of the full-matrix least-squares program ORFLS (Busing, Martin \& Levy, 1962) and GEOM, L. W. Muir \& P. Mallinson's program for molecular geometry calculations. The atomic coordinates are given in Table 1.*

[^0]Discussion. The crystal structure of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ consists of $\mathrm{Pb}^{2+}$ ions and $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$tetrahedra (Fig. 1). The $\mathrm{Pb}^{2+}$ ion is surrounded by seven O atoms belonging to seven different $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$groups, five at short distances and two further away. The next O atom is $3 \cdot 13 \AA$ from the $\mathrm{Pb}^{2+}$ ion, and probably involves a van der Waals contact. The coordination polyhedron is irregular. By sharing the edges $\mathrm{O}(3)-\mathrm{O}(3)$ and $\mathrm{O}(8)-\mathrm{O}(8)$, the coordination polyhedra form infinite chains running in the $y$ direction (Fig. 2). The distance between Pb atoms in the chain is $3.917 \AA$.

Comparison of the crystal structures of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ and $\mathrm{Sn}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ (Herak, Prelesnik, Čurić \& Vasić, 1978) shows that in both compounds the coordination polyhedra of the metal ions form infinite chains instead of the layers that are present in the structures of PbO and SnO . However, in $\mathrm{Sn}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ the coordination of $\mathrm{Sn}^{2+}$ is very similar to that in tetragonal SnO , while in $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ the coordination around $\mathrm{Pb}^{2+}$ is much more complicated than in both forms of PbO . Nevertheless, the geometry of PbO is retained in the structure of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$; four of the five shorter $\mathrm{Pb}-\mathrm{O}$ bonds generally show the same basic pattern of PbO .


Fig. 1. View of the structure of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ down the $b$ axis. Dotted lines represent hydrogen bonds (distances are in $\AA$ ). The dashed circles represent atoms belonging to a phosphate group below.


Fig. 2. The chains of Pb coordination polyhedra. The transformation notation is as in Table 2.

Table 2. Selected interatomic distances ( $\AA$ ) and angles ${ }^{\circ}$ )
(a) Pb coordination polyhedron

| $\mathrm{Pb}-\mathrm{O}(1)^{1}$ | $2.880(14)$ | $\mathrm{Pb}-\mathrm{O}(5)$ | $2.758(16)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Pb}-\mathrm{O}(3)$ | $2.494(15)$ | $\mathrm{Pb}-\mathrm{O}(8)^{1}$ | $2.444(14)$ |
| $\mathrm{Pb}-\mathrm{O}(3)^{1}$ | $2.581(14)$ | $\mathrm{Pb}-\mathrm{O}(8)^{\text {vil }}$ | $2.570(14)$ |
| $\mathrm{Pb}-\mathrm{O}(4)^{\text {lii }}$ | $2.567(14)$ |  |  |

$\mathrm{Pb}-\mathrm{O}(4)^{\mathrm{III}} \quad 2.567(14)$
(b) The geometry of the phosphate groups

| $\mathrm{P}(1)-\mathrm{O}(1)$ | $1.564(15)$ | $\mathrm{P}(2)-\mathrm{O}(5)$ | $1.517(16)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{P}(1)-\mathrm{O}(2)$ | $1.597(15)$ | $\mathrm{P}(2)-\mathrm{O}(6)$ | $1.586(18)$ |
| $\mathrm{P}(1)-\mathrm{O}(3)$ | $1.534(16)$ | $\mathrm{P}(2)-\mathrm{O}(7)$ | $1.531(16)$ |
| $\mathrm{P}(1)-\mathrm{O}(4)$ | $\mathrm{I} .548(16)$ | $\mathrm{P}(2)-\mathrm{O}(8)$ | $1.507(13)$ |
| $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(2)$ | $102.3(6)$ | $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(6)$ | $105.7(6)$ |
| $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(3)$ | $104.2(7)$ | $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(7)$ | $108.3(7)$ |
| $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(4)$ | $112.1(8)$ | $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(8)$ | $114.3(6)$ |
| $\mathrm{O}(2)-\mathrm{P}(1)-\mathrm{O}(3)$ | $110.9(7)$ | $\mathrm{O}(6)-\mathrm{P}(2)-\mathrm{O}(7)$ | $109.7(6)$ |
| $\mathrm{O}(2)-\mathrm{P}(1)-\mathrm{O}(4)$ | $109.1(8)$ | $\mathrm{O}(6)-\mathrm{P}(2)-\mathrm{O}(8)$ | $107.6(7)$ |
| $\mathrm{O}(3)-\mathrm{P}(1)-\mathrm{O}(4)$ | $117.2(8)$ | $\mathrm{O}(7)-\mathrm{P}(2)-\mathrm{O}(8)$ | $111.2(6)$ |

(c) $\mathrm{O} \cdots \mathrm{O}$ distances including hydrogen bonds

| $\mathrm{O}(1) \cdots \mathrm{O}(4)^{\mathrm{vv}}$ | $2.64(2)$ | $\mathrm{O}(5) \cdots \mathrm{O}(5)^{\mathrm{v}}$ | $2.44(2)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{O}(2)^{1 i n} \cdots \mathrm{O}(7)$ | $2.64(2)$ | $\mathrm{O}(7) \cdots \mathrm{O}(7)^{\mathrm{vi}}$ | $2.46(2)$ |

$\mathrm{O}(6)^{\mathrm{vil}} \ldots \mathrm{O}(2)^{\mathrm{II}} \quad 2.74$ (2)
Symmetry code

| (i) | $-x,-y,-z$ | (v) | $-x,-y, 1-z$ |
| :--- | ---: | :---: | :---: |
| (ii) | $1-x, 1-y, 1-z$ | (vi) | $1-x,-y, 1-z$ |
| (iii) | $-x, 1-y,-z$ | (vii) | $x, y+1, \quad z$ |
| (iv) | $1-x, 1-y,-z$ |  |  |

The geometries of the two unique $\mathrm{PO}_{4}^{-}$groups are given in Table 2. The $\mathrm{P}(1) \mathrm{O}_{4}$ group is coordinated to three different $\mathrm{Pb}^{2+}$ ions through the $\mathrm{O}(1) \cdots \mathrm{O}(3)$ edge, $\mathrm{O}(3)$ and $\mathrm{O}(4)$. The $\mathrm{P}(2) \mathrm{O}_{4}$ group is also coordinated to three $\mathrm{Pb}^{2+}$ ions, through the apices $\mathrm{O}(5)$ and $\mathrm{O}(8)$, the latter being coordinated to two $\mathrm{Pb}^{2+}$ ions related by an inversion centre.

The $\mathrm{O} \cdots \mathrm{O}$ distances between neighbouring phosphate groups indicate clearly the positions of the H atoms and hence the hydrogen-bond network (Table 2).

Two short, symmetrical hydrogen bonds exist between symmetry-related atoms $\left[\mathrm{O}(5) \cdots \mathrm{O}(5)^{v}\right.$ and $\left.\mathrm{O}(7) \cdots \mathrm{O}(7)^{\mathrm{vi}}\right]$ forming chains of $\mathrm{H}_{2} \mathrm{P}(2) \mathrm{O}_{4}^{-}$tetrahedra parallel to the $x$ axis. The $\mathrm{O}(1) \cdots \mathrm{O}(4)^{\text {lv }}$ hydrogen bonds link $\mathrm{H}_{2} \mathrm{P}(1) \mathrm{O}_{4}^{-}$tetrahedra into dimers across the inversion centre at $0.5,0.5,0$. These two arrangements of phosphate tetrahedra are linked together by $O(2) \cdots O(7)$ and $O(6) \cdots O(2)$ hydrogen bonds in a three-dimensional network.

The same hydrogen bonding is found in the structures of $\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ (Dickens, Prince, Schroeder \& Brown, 1973) and its arsenate isomorph $\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{AsO}_{4}\right)_{2}$ (Ferraris, Jones \& Yerkess, 1972). The barium analogue $\mathrm{Ba}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$ (Herak \& Krstanović, 1975; Gilbert \& Lenhert, 1978) has a two-dimensional network of strong hydrogen bonds, some of them connecting symmetry-related O atoms. The simultaneous presence of symmetrical and nonsymmetrical
hydrogen bonds has also been observed in the crystal structures of $\mathrm{CsH}_{2} \mathrm{PO}_{4}$ (Uesu \& Kobayashi, 1976) and $\mathrm{TlH}_{2} \mathrm{PO}_{4}$ (Oddon, Tranquard \& Pèpe, 1979). The extended linkage of $\mathrm{PO}_{4}$ groups through symmetrical hydrogen bonds suggests a possible ferroelectric behaviour. Because of its remarkable sensitivity to moisture, measurements of dielectric properties and pyroelectric temperature analysis (Topić, 1979) were performed on polycrystalline samples of $\mathrm{Pb}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$. No determinate results could be gathered from these measurements.

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# Structure of Trirubidium Heptachlorodicuprate(II) 

By W. J. Crama<br>Gorlaeus Laboratories, University of Leiden, PO Box 9502, 2300 RA Leiden, The Netherlands

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#### Abstract

Rb}_{3}\left[\mathrm{Cu}_{2} \mathrm{Cl}_{7}\right]\), orthorhombic, Ccca, $T=295$ $\mathrm{K}, a=24.843$ (4), $b=7.216$ (1), $c=7.216$ (1) $\AA, V=$ $1293.59 \AA^{3}, Z=4$. Intensity measurements were made on a four-circle diffractometer. The final $R_{w}$ value is 0.022 for 5448 reflections. The structure of this new phase in the system $\mathrm{RbCl}-\mathrm{CuCl}_{2}$ can be derived from the $\mathrm{Rb}_{3}\left[\mathrm{Mn}_{2} \mathrm{Cl}_{7}\right]$ structure [Amit, Horowitz \& Makovsky (1972). Isr. J. Chem. 10, 715-719]; in addition, the title compound shows a static cooperative Jahn-Teller effect. The $\mathrm{CuCl}_{6}$ octahedra are elongated and order antiferrodistortively in the double layer and between similar double layers.


Introduction. In the phase diagram of RbCl and $\mathrm{CuCl}_{2}$ a new compound was found in an attempt to prepare $\mathrm{Rb}\left[\mathrm{CuCl}_{3}\right]$. Because of the interest of our department in the cooperative Jahn-Teller effect, the structure of this compound could be valuable for understanding the cooperative effects in similar structure types. The related structure of $\mathrm{K}\left[\mathrm{CuF}_{3}\right]$ (Tsukuda \& Okazaki, 1972) is not uniquely defined with respect to the stacking of the CuCl layers. In another related structure, $\mathrm{K}_{2}\left[\mathrm{CuF}_{4}\right]$ (Haegele \& Babel, 1974) there seems to be a unique interaction over quite a longer distance,
but different from that found in $\left(\mathrm{NH}_{4}\right)_{2}\left[\mathrm{CuCl}_{4}\right]$ (Willett, 1964). In these compounds the $\mathrm{Cu}^{2+}$ ions are found in square layers together with $\mathrm{F}^{-}$or $\mathrm{Cl}^{-}$ions. Nearest and next-nearest interlayer interactions between the Jahn-Teller centres seem to be important. Perhaps the structure of $\mathrm{Rb}_{3}\left[\mathrm{Cu}_{2} \mathrm{Cl}_{7}\right]$ can help to clarify the cooperative Jahn-Teller interactions between layers in this kind of structure.

By means of DTA an endothermic transition was found at 495 K . This is also the case in $\mathrm{Rb}_{2}\left[\mathrm{CuCl}_{4}\right]$ ( 495 K) (Witteveen, Jongejan \& Brandwijk, 1974). This could be related to a transition to a Jahn-Teller disordered phase as described by Höck, Schröder \& Thomas (1978). The compound melts/decomposes at 644 K.
Single crystals of $\mathrm{Rb}_{3}\left[\mathrm{Cu}_{2} \mathrm{Cl}_{7}\right]$ were grown in a methyl alcohol solution. A saturated solution of RbCl in methyl alcohol was poured into a $\mathrm{CuCl}_{2}-$ methyl alcohol solution. The latter contains a molar excess ( $10 \%$ ) of $\mathrm{CuCl}_{2}$ and the concentration was such that no immediate crystallization occurred. Both solutions contained some ethyl orthoformate to avoid the formation of hydrates. After several hours dark-brown crystals appeared; these had a bipyramidal shape with


[^0]:    * A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 35774 ( 9 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

